Theoretical modeling and evaluation of the axial resolution of the adaptive optics scanning laser ophthalmoscope

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Abstract. We present axial resolution calculated using a mathematical model of the adaptive optics scanning laser ophthalmoscope (AOSLO). The peak intensity and the width of the axial intensity response are computed with the residual Zernike coefficients after the aberrations are corrected using adaptive optics for eight subjects and compared with the axial resolution of a diffraction-limited eye. The AOSLO currently uses a confocal pinhole that is 80 μm, or 3.48 times the width of the Airy disk radius of the collection optics, and projects to 7.41 μm on the retina. For this pinhole, the axial resolution of a diffraction-limited system is 114 μm and the computed axial resolution varies between 120 and 146 μm for the human subjects included in this study. The results of this analysis indicate that to improve axial resolution, it is best to reduce the pinhole size. The resulting reduction in detected light may demand, however, a more sophisticated adaptive optics system. Our model includes large pinholes are relatively insensitive to misalignment in the lateral positioning of the confocal pinhole. However, when small pinholes are used to maximize resolution, alignment becomes critical. © 2004 Society of Photo-Optical Instrumentation Engineers. [DOI: 10.1117/1.1627775]

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1 Introduction

Confocal imaging systems are attractive because of their enhanced three-dimensional imaging capability. The optical system images light scattered from the regions in the neighborhood of the focal plane and this is focused onto a pinhole. The confocal pinhole selectively allows light from a specific thickness of the object to be imaged onto the detector. This enables us to axially section the specimen and generate a three-dimensional view of the specimen itself. Wilson discusses at length the role of the pinhole in confocal imaging systems. His analysis was for a scanning laser microscope, and the treatment of aberrations was limited to low-order aberrations only (astigmatism, primary coma, and spherical aberration), which are the only aberrations that are typically present in manufactured optical systems. Our model includes myriad aberrations that can be present in the eye, albeit to a smaller degree, even after correction with adaptive optics (AO). Another important distinction between Wilson’s analysis and ours is that he concentrated on imaging perfect reflectors, rather than diffuse reflectors. A specular reflection retains the phase information that is induced in the first pass of light into the system, whereas a diffuse reflection does not. In the human eye, the retina best approximates a diffuse reflector, so that our diffuse reflection model is more appropriate for modeling the performance of the ophthalmoscope.

Unlike conventional imaging systems, the scanning laser imaging system discussed in this paper is a double-pass imaging system, which uses identical optics for illumination and observation. Brakenhoff and Muller discuss the advantage of a double-pass system and have shown that the full width at half maximum (FWHM) of the point spread function (PSF) of a double-pass system is smaller than that of a single-pass imaging system. For example, in confocal systems with small pinholes, the lateral resolution is about 40% better than conventional diffraction-limited imaging. However, image quality in double-pass scanning imaging systems is degraded by aberrations in the same way as conventional imaging systems. In scanning laser ophthalmoscopy, the main source of aberrations is the eye itself, which serves as the objective lens. To overcome the image degradation from ocular aberrations, Roorda et al. incorporated AO into a scanning laser ophthalmoscope (SLO), the instrument will be hereafter referred to as the AOSLO, and they were able to provide the first real-time images of photoreceptors and blood flow in the human retina.

The goal of this work is to model and understand the benefits that AO provides to a scanning laser ophthalmoscope, specifically with respect to its ability to enhance efficiency in light detection and improve axial and lateral resolution. We are concerned with the impact of residual aberrations because AO systems do not necessarily correct all the aberrations of the eye. In our opinion, the performance of an AO confocal imaging system depends on two things: (1) the effectiveness of the AO system in correcting for the aberrations and (2) the choice of the appropriate confocal pinhole. The strength of the...
AO incorporated in the conventional scanning laser ophthalmoscope lies in the fact that the higher-order aberrations are corrected and hence the PSF is much narrower, resulting in an improved resolution as well as a greater concentration of photons through the confocal pinhole. When the object is in the focal plane, the light scattered from the object is focused onto the pinhole and the signal is detected. If the object is positioned out of the focal plane and a defocused spot is formed on the pinhole, then the intensity measured in the detector is greatly reduced. In either case, the structure of the PSF determines the amount of light getting through the pinhole. In the following sections, we describe the model developed to calculate the axial resolution of the AOSLO and discuss the results obtained using such a model.

2 Model-Based Axial Resolution Calculation for the AOSLO

The computation of the axial resolution involves three stages: (1) computing the single-pass PSF on the retina, (2) re-imaging the PSF in the retina to the confocal pinhole plane, and (3) computing the amount of light that passes through the confocal pinhole (which depends on the pinhole size). An unfolded optical diagram of the system is shown in Fig. 1. Each stage is described here. To simplify the analysis, the model uses a magnification of unity between the source, the retina, and the confocal pinhole.

The calculation models a condition where a flat, diffuse reflector is moved through the focal plane of the SLO. This is not the only metric to define axial image quality (for example, one might choose to quantify the resolution between two axially separated point sources), but it is commonly used and it is easily measured in an experimental setting.

2.1 Stage 1: Image Formation on the Retina

Wave aberrations are two-dimensional functions that can be decomposed into Zernike polynomials, separable in angle and radius, and written in orthogonal form as

\[ \phi(r, \theta) = \sum_{n=0}^{\infty} a_n z_n(r, \theta), \]

where \( n = 0, 1, 2 \) are piston and tilt components, respectively, and \( a_n \) are the coefficients of the corresponding Zernike polynomial \( z_n \) (ordered according to the standards proposed for use in vision science). The phase map of the wavefront for each subject in the study is computed from actual wave aberrations, represented by Zernike polynomials. For the diffraction-limited eye, all the Zernike coefficients are set to zero and hence the PSF is the diffraction-limited PSF of the system itself.

The AO system in the AOSLO consists of a wavefront sensor for measuring the wave aberrations and a deformable mirror for compensating for the aberrations. A Shack Hartmann wavefront sensor is used to measure the wavefront slopes, and these slopes are modeled using these Zernike polynomials. Based on these coefficients, the appropriate signals are then sent to a deformable mirror to compensate for the aberrations. The sampling of the wavefront by the wavefront sensor and the number of degrees of freedom in the deformable mirror determine the level of wavefront correction, especially the higher orders. In the AOSLO, the wavefront is sampled at 241 locations over a 6.3-mm pupil and the deformable mirror has a continuous surface supported by 37 actuators. After AO correction, we are left with the residual aberrations, which prevent us from reaching the ideal diffraction-limited performance. In our model, these residual aberrations are used to estimate the achievable axial resolution. Phase maps are generated using the residual Zernike coefficients after wavefront compensation using AO. In our case, the Zernike coefficients are calculated for a 6.3-mm pupil, which is the pupil size used most often in the Houston AOSLO. Using the coordinate system in Fig. 1, assuming that the aberrations are introduced in the \((\alpha, \beta)\) plane, the point spread function at the retinal plane is given by the Fourier transform of the phase map.

\[ p_r(x_r, y_r) = FT \left[ P(\alpha, \beta) \times \exp \left\{ - \frac{2\pi}{\lambda} i \phi(\alpha, \beta) \right\} \right], \]

where \( P(\alpha, \beta) \) is a function defining the shape and size of the pupil, and \( \phi(\alpha, \beta) \) is the wave aberration function, cast into Cartesian coordinates. The intensity PSF in the retinal plane is

\[ I_{psf} = p_r p_r^*, \]

where \(^*\) represents the complex conjugate.

2.2 Stage 2: Imaging the Retinal PSF at the Plane of the Confocal Pinhole

The AOSLO is a double-pass imaging system in which the same pupil size is used for illumination as well as light collection. The intensity distribution at the confocal pinhole plane is simply an image of the PSF that landed on the retina (assuming that the retina is a uniform diffuse reflector). When the pupil size for retinal illumination and light collection is the same, the intensity distribution at the plane of the confocal pinhole turns out to be the autocorrelation of the single-pass PSF. Moving the retina forward or backward slightly results in a defocused single-pass PSF. Under such conditions, the double-pass PSF is still the autocorrelation of the (defocused) single-pass PSF because the light collection path suffers from the same defocus as the illumination path, and hence has the same PSF. Therefore, the double-pass PSF \( I_{dpsf} \) measured at the image plane \((x, y)\) is
\[ I_{dpssf}(x_i, y_i, z_r) = \int_{x_i}^{x_i+1} \int_{y_i}^{y_i+1} I_{psf}(x', y', z_r) I_{psf}(x' + x_i, y') \, dx' \, dy', \]

(4)

where \( I_{psf} \) and \( I_{dpssf} \) are the intensities of the single-pass PSF and double-pass PSF at some fixed axial plane at a distance \( \pm z_r \) on either side of the zero defocus plane.

**2.3 Stage 3: Integrating the Light through the Confocal Pinhole**

If \( c(x_i, y_i) \) is a circ function representing the confocal pinhole, with the principal axis of the optical system passing through its center with \((x_0, y_0)\) defining the origin in the \((x_i, y_i)\) plane, the total integrated intensity \( I \) at different axial positions is

\[ I(z_r) = \int_{x_i}^{x_i+1} \int_{y_i}^{y_i+1} c(x_i, y_i) I_{dpssf}(x_i, y_i, z_r) \, dx \, dy, \]

(5)

where \( I_{dpssf}(x_i, y_i, z_r) \) is the double-pass point spread function estimated at various defocus planes along \( z_r \), and the confocal pinhole defined over a diameter \( a \) in the \((x_0, y_0)\) plane. In the equation for \( I(z_r) \), it is assumed that all of the light passing through the pinhole is detected. The FWHM of the axial intensity response \( I(z_r) \) is a measure of the axial resolution of the system.

In order to relate changes in defocus to changes in actual distance, we used a reduced eye model with a power of 60 D and an index of refraction of 1.333 having an emmetropic secondary focal length of 22.2 mm. Although the reduced eye is a poor approximation for a human eye, the important parameter for our computation, the numerical aperture, is about the same. For example, for a 6-mm pupil, the Gullstrand-Emsley schematic eye (described in Ref. 10), which is a more realistic schematic eye, and the reduced eye have numerical apertures of 0.176 and 0.175, respectively. Therefore it is appropriate to use a reduced eye model for axial and lateral resolution calculations.

The Zernike coefficients are obtained over a time \( t \), so that \( \tilde{z}_n \) used in our axial resolution calculations is

\[ \tilde{a}_n = \langle \tilde{a}_n(t) \rangle, \]

(6)

where \( n = 0, 1, 2, \ldots, k \) (in the AOSLO \( k = 65 \)) and \( \langle \ldots \rangle \) denotes the time average of the Zernike coefficients computed from the slope measurements of the wavefront sensor obtained in real time in the AOSLO.\(^5\) The root mean square value (r.m.s.) of the Zernike modes, which is the r.m.s. of the wavefront, is computed using the formula,

\[ \text{r.m.s.} = \left[ \sum_n (\tilde{a}_n)^2 \right]^{1/2}. \]

(7)

The average r.m.s. of the eight subjects after AO correction are as follows:

<table>
<thead>
<tr>
<th>Subjects</th>
<th>Average r.m.s.</th>
</tr>
</thead>
<tbody>
<tr>
<td>a1</td>
<td>0.040 ( \mu )m</td>
</tr>
<tr>
<td>a2</td>
<td>0.051 ( \mu )m</td>
</tr>
<tr>
<td>a3</td>
<td>0.084 ( \mu )m</td>
</tr>
<tr>
<td>a4</td>
<td>0.065 ( \mu )m</td>
</tr>
<tr>
<td>a5</td>
<td>0.079 ( \mu )m</td>
</tr>
<tr>
<td>a6</td>
<td>0.096 ( \mu )m</td>
</tr>
<tr>
<td>a7</td>
<td>0.104 ( \mu )m</td>
</tr>
<tr>
<td>a8</td>
<td>0.142 ( \mu )m</td>
</tr>
</tbody>
</table>

Calculations were done for a wavelength of 660 nm. To get proper scaling between the double-pass PSF and the physical pinhole size, we modeled a numerical aperture of the image-collecting optics of 0.03. These factors were chosen to imitate the optical system currently used in the Houston AOSLO.

**3 Lateral Positioning of the Confocal Pinhole and its Effect on Axial Resolution Measurements**

Any misalignment in the lateral positioning of the confocal pinhole with respect to the rest of the optics may significantly affect the high-resolution imaging capabilities of the instrument. In the following section we compute the effect of misalignment of the confocal pinhole. We introduce a known amount of misalignment in our computational model and calculate the total intensity at the detector arm, as well as the width of the axial intensity response.

If \((x_k, y_0)\) defines the origin in the \((x_i, y_i)\) plane, then the intensity \( I \) at a defocus position \( z_r \) with a misalignment \( x_0 \) \( \pm x_i \) is given by Eq. (5), with the confocal pinhole centered at \((x_k, y_0)\).

**4 Results**

**4.1 Axial Resolution of the Theoretically Modeled AOSLO**

The model calculations were performed and the FWHM of the axial spread function was obtained for pinholes of different diameters. The plots show the pinhole diameter expressed as a percentage relative to the pupil diameter, and its effect on the axial spread function. The plots show the pinhole diameter expressed in units that are normalized to the radius of the Airy disk of the optical system. This normalization facilitates the interpretation of the results and allows a direct comparison between similar instruments. With the pinhole sizes normalized in this way, one can easily compute actual pinhole sizes, or the pinhole size projected into retinal coordinates, using the following equation:

\[ r_a = 1.22 \frac{\lambda f}{n d} m, \]

(8)

where \( \lambda \) is the wavelength of light, \( f \) is the focal length, \( n \) is the index of refraction of the media in which the light is focused, and \( d \) is the diameter of the beam forming the image. For example, in the Houston AOSLO, the collector lens in front of the confocal pinhole (in air) has a focal length \( f \) of 100 mm and the beam diameter at this lens is 3.5 mm \( (d) \); hence the radius of the Airy disk at the confocal pinhole \( r_a \) is 23 \( \mu \)m. The pinhole projects into the reduced eye retinal space \((6.3 \text{ mm pupil diameter}) \) as 2.13 \( \mu \)m. In the Houston...
AOSLO, we often use a pinhole size of 80 μm, which converts to 3.48 Airy disk units and projects to 7.41 m. The subject had an initial r.m.s. wave aberration of 0.60 μm; after AO correction it was reduced to 0.11 μm.

The FWHM of an axial intensity response estimated for different pinhole diameters. Residual aberrations after AO correction determine the axial resolution. The line with short dashes is for a subject who had not been corrected with AO and who had an r.m.s. wave aberration of 0.53 μm. The line with long dashes is for a diffraction-limited model eye, and the solid lines are for the eight subjects after the best AO correction.

The axial intensity response curves calculated for a typical subject imaged with and without AO using a 23- and an 80-μm pinhole are shown in Fig. 2. The initial r.m.s. without AO is 0.60 μm and the mean r.m.s. after the AO correction is applied is 0.11 μm. For a 23-μm pinhole, we could see at least a fourfold increase in the axial resolution with AO, and for an 80-μm confocal pinhole, we observed at least a twofold increase in axial resolution with AO. A comparison of the axial intensities with and without AO obtained using a 23-μm confocal pinhole shows at least an eightfold increase in the peak intensity of the axial spread function with AO, and an 80-μm confocal pinhole shows at least an eightfold increase in the peak intensity of the axial spread function with AO compared with that obtained without AO.

Figure 3 shows a plot of the peak intensity of an axial intensity profile for different pinhole diameters. The line with short dashes is for a subject who had not been corrected with AO and who had an r.m.s. wave aberration of 0.53 μm. The line with long dashes is for a diffraction-limited model eye, and the solid lines are for the eight subjects after the best AO correction.

Theoretical modeling and evaluation of the axial resolution...
When the r.m.s. of the wave aberration is less than $\frac{\lambda}{2p}$, the Strehl ratio is given approximately by the expression:

$$\max(I_{\text{dpsf}}) / \max(I_{\text{dpsf}(f=0)}) \approx \exp\left[-\frac{2\pi^2}{\lambda} (\text{r.m.s.})^2\right].$$

Where $I_{\text{dpsf}}$ is the maximum intensity of the PSF with residual aberrations after AO correction, $I_{\text{dpsf}(f=0)}$ is the maximum intensity in the diffraction-limited case, and $\lambda$ is the wavelength of light used for imaging. For an AO-corrected wavefront, it is safe to assume that r.m.s. $< \frac{\lambda}{2\pi}$ and the r.m.s. is calculated as described in Eq. (7).

Figure 6 is a scatter plot of the peak intensity of the axial intensity response curves calculated from the residual aberrations versus the FWHM of the axial intensity response. Figure 7 is a scatter plot of the Strehl ratio $\max(I_{\text{dpsf}})/\max(I_{\text{dpsf}(f=0)})$ calculated directly from the r.m.s. wave aberrations versus the FWHM of the axial intensity response of the subjects in our study for an 80-μm confocal pinhole. We can see that the axial resolution of a subject is proportional to the Strehl ratio. From this figure, we also see that the FWHM of the best AO-corrected wavefront can lead to an effective axial resolution of approximately 48 μm and the diffraction limit is approximately 45 μm for a confocal pinhole of a size equal to the Airy disk radius of the AOSLO; however, the peak intensity drops off by approximately 50%. Assuming that photon noise is the only source of noise, the signal-to-noise ratio in the image reduces by about $\sqrt{2}$ times the signal-to-noise ratio obtained using an 80-μm confocal pinhole.

Fig. 5 The residual r.m.s. of Zernike orders of eight different subjects used in our study. The panel is arranged in order of decreasing axial resolution for different subjects whose axial resolution was computed from these residual Zernike coefficients.

Fig. 6 A scatter plot of the FWHM of the axial intensity response of different subjects versus the normalized peak intensity of the axial intensity response (measure of Strehl ratio) for an 80-μm confocal pinhole and for a 23-μm confocal pinhole, which is the Airy disk radius of the collection optics of the AOSLO. The peak intensities are normalized to the peak intensity of the axial intensity response of the diffraction-limited model eye.

Fig. 7 A scatter plot of the FWHM of the axial intensity response of different subjects versus the Strehl ratio computed from the residual wave aberrations for an 80-μm confocal pinhole and for a 23-μm confocal pinhole, which is the Airy disk radius of the collection optics of the AOSLO.
4.2 Effect of Lateral Misalignment of the Confocal Pinhole

To investigate the role of a misaligned pinhole, we do the following: Misalignments in the pinhole ranging from 0 to 5 μm are introduced by laterally displacing the pinhole on either side of the optical axis, and the axial intensity response is calculated. After AO correction, the PSF at the confocal pinhole is compact and symmetric and therefore it affects the axial resolution symmetrically for any misalignment on all directions in the confocal pinhole plane.

Figure 8 shows the point spread function at the confocal pinhole plane with and without AO. The percentage of intensity getting through the confocal pinhole to the detector plane is calculated and normalized to the intensity at the detector plane at zero misalignment. Figure 9 shows, on one hand, the FWHM of the axial intensity response for 23- and 80-μm diameters of the confocal pinhole plotted as a function of the misalignment of the confocal pinhole. Figure 10 is, on the other hand, the plot of the percentage decrease in intensity for misalignments from 0 to 5 μm for different pinhole sizes for (1) the subject with highest residual r.m.s. (2) the subject with the lowest residual r.m.s. and (3) for the diffraction-limited eye. Figures 9 and 10 demonstrate, however, that only the small pinhole is sensitive to misalignments. Axial resolution degrades and intensity drops rapidly with small misalignments with the smaller confocal pinhole. In the case of a 23-μm confocal pinhole, for the subject with the highest residual aberrations there is about an 80% increase in FWHM compared with the FWHM at zero misalignment (decrease in axial resolution), and a corresponding drop in detected intensity of about 70% for a misalignment of 5-μm in the pinhole position. For the 80-μm confocal pinhole, small misalignments cause small improvements in the axial resolution and only a negligible drop in detected intensity.

5 Discussion

The results presented here represent important reference information that will guide our efforts toward optimizing the AOSLO for maximum imaging performance. The main outcome of the study is that the residual levels of aberration left after AO corrections do not impose a large limitation on axial resolution performance. Figure 3 shows that on average, the axial resolution for the AO-corrected eyes is ~129 μm, which is 12% worse than the no-aberration case (for an 80-μm pinhole). Rather, the main limit to axial resolution is imposed by the size of the confocal pinhole. For pinhole sizes that are larger than the radius of the Airy disk of the collection optics, the pinhole size and FWHM of axial resolution are linearly related. However, the residual levels of aberrations after AO correction do cause large losses in the amount of light that can be detected. On average, the decrease in intensity with an 80-μm pinhole is ~30% compared with the aberration-free eye. For high-magnification ophthalmoscopy, a decrease in the detected light levels is a concern because retinal safety imposes limits on how much light can be used to illuminate the retina and the retina is a very weak reflector. In the Houston AOSLO, we operate with light levels that are well below hazardous levels, and because the retina is such a weak reflector, our dominant noise source is photon noise. Therefore, improving axial resolution by using smaller confocal pinholes may be facilitated only by improved performance of the AO system. Improvements in AO performance can be achieved through real-time AO operation and/or by having a
higher number of actuators for correcting higher-order aberration modes, both of which have been demonstrated to improve performance in the Rochester second-generation adaptive optics ophthalmoscope, which is a conventional imaging system without axial slicing capabilities.\textsuperscript{14}

We showed that when the aberrations are low, the axial resolution is linearly related to the Strehl ratio, whether calculated from the r.m.s. of the residual wave aberration, or from the PSF itself. This result demonstrates that after AO correction, the r.m.s. alone should be sufficient to predict the experimental axial resolution. We are planning to do experiments to test this hypothesis.

The subjects whose axial resolution is higher in our calculation (a smaller FWHM) have correspondingly higher peak intensities of the axial resolution profile. This may not be the case in an experiment since the absorption of photons by the retina varies among individuals,\textsuperscript{13} and this has not been taken into account in our calculations. Therefore, the axial intensity profile discussed here depends only on the aberrations and not on the reflective properties of the retina for a specific subject. Based on the reflective quality of the retina, the confocal pinhole diameter can be chosen for the best possible axial resolution to obtain a reasonable signal-to-noise ratio in the images.

Using smaller confocal pinholes will improve axial resolution, but the requirement for a better optical alignment between the confocal pinhole and the rest of the optical system can inhibit obtaining images with a good signal-to-noise ratio. The demands on alignment of the confocal pinhole are higher as the confocal pinhole diameter gets closer to the Airy disk radius, for which we see significant drops in peak intensity with misalignments of a few micrometers (Fig. 10). We can also see that when the pinhole diameter is considerably larger than the Airy disk radius, the effects of pinhole misalignment are less significant, for both intensity and resolution. It is worth noting here that in some cases, the axial resolution can improve slightly with a pinhole misalignment, at little cost to the peak detected intensity.

All calculations have been done assuming a plane diffuse-reflecting object with isotropic reflectivity and a reduced model eye with no absorption and no scattering. However, no plane diffuse-reflecting features exist in the retina. In previous reports, axial resolution has been reported for features such as blood vessels\textsuperscript{6,15} and the surface of the nerve fiber layer,\textsuperscript{7,16} which only approximate diffuse reflectors. The actual resolution that one will obtain will depend on the specific retinal feature, and therefore the ability to resolve layers in axial depth for that specific feature may be worse than what is reported here.

6 Conclusions

We have discussed in this paper a theoretical model developed to optimally choose the confocal pinhole to improve the axial sectioning capabilities of an AO scanning laser ophthalmoscope. The optimal confocal pinhole choice will be the one for which the axial spread function has a small FWHM and a high peak intensity. For example, with the present AOSLO, if an axial resolution of 60 \( \mu m \) is desired, then the confocal pinhole diameter would have to be about 35 \( \mu m \) (1.5 times the Airy disk radius), but in our current system this would result in a relative reduction in peak intensity to 30% compared with what would be detected through large pinholes. Only superior AO performance can help us achieve lower axial resolution without appreciable loss in intensity. We have also shown that since the AO-corrected r.m.s. wave aberration is low (r.m.s. \( <\lambda/2\pi \)), we are in a regime where r.m.s. values alone can be a good predictor of the axial resolution.

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