Comparison of sea-level measurements between microwave radar and subsurface pressure gauge deployed at select locations along the coast of India

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Abstract. Sea-level data are obtained from several remote and coastal locations using absolute pressure gauges deployed at known level, known as chart datum. However, to yield correct sea-level measurements from absolute pressure measurements, it is necessary to take into account the atmospheric pressure and water density at the measurement locations. We used data collected from microwave radar and an absolute pressure gauge deployed at Verem, Goa (January 2009 to May 2010), Tuticorin, and Mandapam, Tamil Nadu (June 2010 to March 2011) to carry out comparative studies. The root-mean-square difference between the estimated sea level from radar and pressure gauge (incorporating atmospheric pressure correction) is \( \sim 2.69 \), 2.73, and 1.46 cm at Verem, Tuticorin, and Mandapam, respectively. Harmonic analysis of the two time-series of sea-level data at Verem produces similar residuals and tidal constituents. Our results indicate the importance of concurrent measurement of atmospheric pressure along with subsurface absolute pressure gauge measurements. Internet-based real-/near-real-time tracking and monitoring of sea level, sea state, and surface-meteorological conditions from a network of several island and coastal stations provides considerable information to disaster managers and local administrators during episodic events such as storms, storm surges, and tsunamis.

1 Introduction

Information on sea level and its variability along coastal locations is essential for operational applications as well as scientific studies. Apart from safer navigational and coastal management activities at local level, sea-level data are also needed for measuring and predicting storm surges, understating the current sea-level variability and its implications to the coastal population (e.g., Refs. 1 and 2), validating sea-level models and calibrating satellite radar altimeters (e.g., Refs. 3–5). On a global scale, real-time sea-level studies are crucial to understand the changes in the Earth’s climate and its multidecadal fluctuations (e.g., Refs. 6–8). The average global sea-level rise, which is consistent with warming, is estimated at an average rate of 1.8 (1.3 to 2.3) mm per year over the period of 1963 to 2003.9 However, the disastrous consequences of the recent Japan tsunami (March 11, 2011), impact of the powerful December 2004 global tsunami,10,11 and the historically known vulnerability of the Indian coasts to storm surges12 emphasize the need for real-/near-real-time reporting of sea level, sea state, and surface-meteorological information for multihazard monitoring and warning purposes. Although a single system at a given location may not be of much practical use for warning, a network of spatially distributed real-/near-real-time reporting gauges in the coastal and island locations will be greatly beneficial to disaster managers and local administrators because a signal of any natural event
takes time to travel from the source region to a distant location. In such a situation, a network of real-/near-real-time reporting gauges will allow monitoring of the progress of the event, helping the decision-makers to take necessary precautions.

The December 2004 Indian Ocean tsunami episode prompted all countries with ocean boundaries to prepare for a possible disaster due to tsunamis and storm surges. Since then, many countries have developed and deployed deep-ocean tsunami monitoring systems and networks of real-time monitoring coastal sea-level gauges; other countries are in the process of establishing such systems. It is prudent for countries with coastlines vulnerable to tsunamis and storm surges to have prior knowledge of technologies that are suitable for their specific needs. As many of the countries that are threatened by tsunamis are resource-limited, choosing the wrong or inappropriate technology may lead to heavy casualties during the next episode. A comprehensive description that offers an unbiased comparative evaluation and assessment of the optimum technology suitable for specific situations is given by Joseph,13 Martin et al.,14,15 Kranz et al.,16 and Woodworth and Smith17 reported the test results of radar tide gauges manufactured by different firms and comparison between other types of gauges. Thus, relative performance of different systems and evaluation of technologies serve as a reference to the personnel responsible for protecting the coastal population.

In this paper, we report the experience gained in developing and operating an Integrated Coastal Observation Network (ICON), which is Internet accessible and provides cellular-based real-/near-real-time sea level, sea state, and surface meteorological observations, established by the Council of Scientific and Industrial Research–National Institute of Oceanography (CSIR-NIO), Goa, India, at several locations on the Indian coasts and islands [Fig. 1(a); http://inet.nio.org]. The first real-/near-real-time reporting cellular-based sea-level station was established in Verem, Goa, in September 2005. The present study is aimed at comparing the sea-level measurements from the downward-looking aerial microwave radar and pressure gauge and evaluating the importance of atmospheric pressure variability in estimating the sea level using subsurface absolute pressure gauges at Verem in Goa and Tuticorin and Mandapam in Tamil Nadu, India. In Sec. 2, we briefly address the theory of pressure and radar gauge (RG) systems, and in Sec. 3, we briefly describe the means and methods for comparative analysis; the results of analysis are presented in Sec. 4.

2 Sea-Level Measurement Methods

The most common sea-level measuring technologies are stilling-well and float, pressure system, acoustic system, and radar system.18 In this section, we briefly describe the principle of operation of pressure and RG systems.

2.1 Pressure Gauge

These systems measure the subsurface pressure [Fig. 2(a)] according to the following law:

\[ h = \frac{(p - p_a)}{\rho \times g}, \]  

where \( h \) is the height of the instantaneous sea surface above the pressure port, \( p \) is the measured subsurface pressure, \( p_a \) is the atmospheric pressure, \( \rho \) is the water density, and \( g \) is Earth’s gravitational acceleration. Therefore, this system requires knowledge of local atmospheric pressure, water density, and local gravity. The density \( \rho \) is important in estuarine waters, as it undergoes seasonal variability due to changes in fresh water influx as well as semi-diurnal variability of tidal cyclicity. In such cases, density corrections need to be incorporated during postprocessing. However, in locations where the water is well mixed, density can be considered constant. The pressure gauge at Verem jetty uses pressure sensor from Honeywell Inc. (Table 1) and is deployed \( \sim 1 \) m below the chart datum (CD) with its electronics, power supply, and solar panel at the top of the mounting structure fixed to the jetty as shown in Fig. 2(a). The
self-recording-type pressure gauges from Sea-Bird Electronics Inc. with metallic housing were deployed near the RGs, resting on the sea bed (depth \( \sim 2 \text{ m} \)) at Tuticorin and Mandapam. The metallic housing of the pressure gauge acted as dead weight (\( \sim 50 \text{ kg} \)) to minimize the drift of the gauges; it was anchored with chains to the nearby jetty.

### 2.2 Radar Gauge

The radar sensor is positioned [Fig. 2(b)] well above the highest expected sea level (also the highest expected wave to avoid damages to the unit) and measures the aerial distance from the sensor to the water surface. Radar is a noncontact device that is capable of remote measurement of sea-level elevation from the air. The transmission frequency of the radar sensor is \( \sim 24 \text{ GHz} \) and the beam width is \( \sim \pm 5 \text{ deg} \). The basic premise involved in the operation of the radar sensor is transmission of microwave pulses toward the sea surface and reception of the reflected/backscattered energy. The reflected microwaves are analyzed to estimate the aerial distance traveled by a given pulse. Averaging over 30 s filters out short-period variability due to wind-waves and swells. Sea-level elevation \((H)\), referenced to CD, is obtained by subtracting the measured aerial distance \((L)\) from the height \((K)\), of the radar sensor above CD. The RG has many advantages over the traditional systems,\(^{18}\) as it makes direct measurements of sea level. The effect of density and temperature variations, even in the atmosphere, are unimportant. On
account of these superior qualities, the RG is used as a reference system in the present comparative study.

The typical configuration of subsurface pressure sensors and downward-looking aerial microwave radar gauges incorporated in the ICON are shown in Fig. 3. The sea-level information acquired using dedicated Linux-based data loggers and uploaded to an Internet server using GPRS cellular modems are available in graphical format at http://inet.nio.org. The radar-level sensor from OTT Hydromet GmbH (OTT-RLS) is used in the RGs of ICON in order to meet the national and international needs of sea-level monitoring and compatibility to the Global Sea Level Observation (GLOSS) program. They feature the common characteristics listed in Table 1.

![Fig. 2 Typical installations of (a) subsurface pressure gauge (PG) and (b) downward-looking aerial microwave radar gauge (RG).](image)

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3 Data and Method

In this section, we provide a brief description of the ICON, the data acquired from Verem, Tuticorin, and Mandapam stations and the comparison method used.

3.1 Integrated Coastal Observation Network

The in-house designed and developed Internet-accessible real-/near-real-time reporting cellular-based sea level, sea state, and surface meteorological (Met) stations deployed at several locations
on the Indian coasts and islands is described in detail by Prabhudesai. The network of autonomous weather stations (AWS), sea-level gauges, and wave rider buoys as shown in Fig. 3 are incorporated in the ICON. The sea-level and surface meteorological data are acquired using dedicated Linux-based data loggers and uploaded to an Internet server at 5- and 10-min intervals, respectively, with the use of GPRS cellular modems. The sensors and data loggers are powered from sealed lead acid batteries, which are charged through solar panels (Figs. 2 and 3). The ICON provides graphical presentation of sea-level information [observed sea level, predicted tide, sea-level residual (SLR)] and surface meteorological information (such as vector-averaged wind speed and direction, barometric pressure, atmospheric temperature, relative humidity, solar radiation, and rainfall). The network maintains accurate time-stamp of the dataset through Internet-time synchronization using network time protocol. The ICON provides several benefits, such as remote monitoring of individual stations, remote health monitoring to aid timely maintenance, and periodic arrival of data streams from all stations at a single central server. The ICON data could be assimilated to real-time running of numerical models for operational forecast. The NIO network allows Internet-based real-/near-real-time tracking and monitoring of sea level, sea state, and meteorological conditions along the Indian coasts and islands and from almost anywhere having cellular connectivity. This is of considerable practical significance during natural disasters such as storms, storm surges and tsunamis.

3.2 Data

Sea-level data are collected off Goa [Fig. 1(b)] using real-time reporting pressure and radar gauges at Verem, located near the mouth of the Mandovi estuary, from January 2009 to May 2010. The sea-level gauge instruments are described in detail by Prabhudesai et al. The PG data are sampled at 2 Hz frequency for 5-min durations (600 samples), averaged, and subsequently recorded in the data-logger at every 5 min. The RG samples are acquired over a 30-s window at 1-min intervals and averaged over 5-min intervals. Atmospheric pressure measurements collected from an AWS installed ~5 km away from the sea-level station are used for retrieving sea-level measurements from the absolute pressure (i.e., water pressure + atmospheric pressure) measurements acquired by the subsurface PG. For comparison, we have used time-series data at 10-min intervals. The recording-type PGs deployed at Tuticorin and Mandapam acquired data at an interval of 10 min with an integration duration of 1 min. The AWS was installed at Mandapam near the RG (~500 m) and is ~115 km from Tuticorin. The barometric pressure from this AWS is used for atmospheric pressure correction for both the PGs at Tuticorin and Mandapam, as the atmospheric perturbations have spatial characteristic of a few hundred kilometers (Table 2).

3.3 Comparison Method

To evaluate the accuracy or compare different measurement systems, the difference or error, especially the root-mean-square error (RMSE), is used as the parameter. As discussed by Willmott et al. correlation coefficient ($r$) and its square, the coefficient of determination ($r^2$), may not be consistently related to the accuracy of predictions. Therefore, we compute and report the summary measures such as mean, standard deviation, the intercept, and slope of the least square regression with PG on $y$-axis and RG on $x$-axis. The different measures

<table>
<thead>
<tr>
<th>Station</th>
<th>Location</th>
<th>Distance between RG and PG</th>
<th>Measurement duration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Verem</td>
<td>15.5019° N 73.8121° E</td>
<td>50 m</td>
<td>January 1, 2009 to May 31, 2010</td>
</tr>
<tr>
<td>Tuticorin</td>
<td>08.7499° N 78.2022° E</td>
<td>500 m</td>
<td>June 21, 2010 to March 14, 2011</td>
</tr>
<tr>
<td>Mandapam</td>
<td>09.2713° N 79.1321° E</td>
<td>10 m</td>
<td>June 19, 2010 to March 12, 2011</td>
</tr>
</tbody>
</table>

Table 2 Summary of observations. The data used for analysis are at every 10-min interval and the time is in IST.
are derived from the fundamental quantity \((P_i - O_i)\), where \(P\) is predicted measurements under test and \(O\) is the reference standard. In the present study, the measurements from RG (PG) refer to \(O(P)\). The types of difference measures calculated are briefly defined below (for detailed explanation, please refer to Willmott).\(^{23}\)

Mean absolute error (MAE) \(= \frac{1}{N} \sum_{i=1}^{N} |P_i - O_i|, \) \(2\)

\[
\text{RMSE} = \left[ \frac{1}{N} \sum_{i=1}^{N} (P_i - O_i)^2 \right]^{0.5}, \quad (3)
\]

The systematic portion of the error is written as

\[
\text{RMSE}_s = \left[ \frac{1}{N} \sum_{i=1}^{N} (\hat{P}_i - O_i)^2 \right]^{0.5}, \quad (4)
\]

while the unsystematic part is

\[
\text{RMSE}_u = \left[ \frac{1}{N} \sum_{i=1}^{N} (P_i - \hat{P}_i)^2 \right]^{0.5}, \quad (5)
\]

The index of agreement \((d)\) is of the form

\[
d = 1 - \frac{\sum_{i=1}^{N} (P_i - O_i)^2}{\sum_{i=1}^{N} (|P_i| + |O_i|)^2}, \quad 0 \leq d \leq 1, \quad (6)
\]

where \(N\) is the number of data points, \(\hat{P}_i = a + bO_i\) is the least square regression with the intercept \((a)\) and slope \((b)\), \(P_i^\prime = P_i - \bar{O}\) and \(O_i^\prime = O_i - \bar{O}\).

## 4 Results

Sea-level measurements reported by radar and pressure gauges during January 2009 to May 2010 from Verem, Goa, are shown in Fig. 4. Both the systems reported a tidal range up to 250 cm with fortnightly variation in spring and neap tides [Fig. 4(a) and 4(b)]. The tides off Verem have a "form number" of 0.64, implying that the tides are mixed, mainly of semi-diurnal nature.\(^{24}\) When the tidal signal was removed from the sea-level records using the TASK\(^{25}\) tidal analysis and prediction algorithm, both the systems produced similar SLRs, as shown in Fig. 4(c) and 4(d). The monthly variability is presented in Fig. 5 with negligible difference. The high residual variability (∼163 cm\(^2\)) seen in November 2009 is the response of the sea level to the tropical cyclonic storm Phyan, which developed in winter in the southeastern Arabian Sea and swept northward along the eastern Arabian Sea during November 9 to 12, 2009.\(^{26}\) However, the tidal range at Tuticorin (Mandapam) during the measurement period (Table 1) is ∼125(126) cm [Fig. 6(a), 6(b), 6(d), and 6(e)]. The tides are amplified as they propagate from south to north due to topological/bathymetric variation [Fig. 1(a)]. The mean absolute difference at Tuticorin (Mandapam) is ∼2.1(1.1) cm, as shown in Fig. 6(c) and 6(f) (Table 3).

To evaluate and compare the RGs and PGs, the anomaly (i.e., mean value of the time series) has been removed: scatter plots along with quantitative indices are shown in Fig. 7 (also refer to Table 3). From Fig. 7(a) to 7(c), it is clear that for all the three sites, the slope \((b)\) is 1 and bias \((a)\) is less than 0.6 cm. Also, it appears that the variability of sea level is higher at Tuticorin than Mandapam, with an energy of ∼7.48 and 2.15 cm\(^2\), respectively (Table 4), which may be due to the focusing effect of waves near the southern tip of India. Figure 7(d) to 7(f) show the percentage occurrence of differences at the three sites, respectively. Examination of the summary position and scale parameters (Table 3) of RGs [i.e., mean of RG (RG), standard deviation (S\(_{rg}\))] compares well with the corresponding PGs (i.e., PG, S\(_{pg}\)). The regression parameters

\[
\begin{align*}
&Mehra \text{ et al.: Comparison of sea-level measurements between microwave radar...} \\
&\text{Journal of Applied Remote Sensing} \quad 073569-7 \quad \text{Vol. 7, 2013}
\end{align*}
\]
(a and b) show similar linear observations. MAE at Verem and Tuticorin is ~2 cm; however, at Mandapam it is less (~1.1 cm). RMSE, which results from the square of \( (P_j - O_j) \), tends to inflate when the extreme values are present. RMSE, therefore, can generally be regarded as a high estimate of MAE. RMSE at Verem and Tuticorin is ~2.7 cm and at Mandapam it is ~1.5 cm. RMSE\(_s\) is systematic linear function of differences, and it is ~0.6 cm at Verem and ~0.01 cm at Tuticorin and Mandapam, respectively. With the appropriate parameterization of the model, RMSE\(_s\) can be substantially reduced, and therefore RMSE\(_a\) can be interpreted as a potential measure of accuracy.\(^{25}\) The index of agreement \( (d) \) and the coefficient of correlation \( (r) \) at significance level (95%) is same (0.99) at all the locations. The indices discussed above are listed in Table 3, and they provide a brief evaluation and comparison of PGs and RGs at Verem, Tuticorin, and Mandapam.

We have also estimated tidal constituents from the RG and PG data at Verem, Goa, using harmonic analysis. The basis of harmonic analysis is the assumption that the tidal variations can be represented by a finite number \( n \), harmonic terms of the form\(^{27}\)

![Fig. 4 Sea-level measurements at Goa using (a) RG, (b) PG, and respective residuals from (c) RG and (d) PG.](image)

![Fig. 5 Seasonal sea-level residual variability at Verem, Goa.](image)
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![Graphs showing sea-level measurements and difference](image)

**Fig. 6** Sea-level measurements at Tuticorin using (a) RG, (b) PG, and (c) difference (PG–RG), and at Mandapam using (d) RG, (e) PG, and (f) difference (PG–RG).

**Table 3** Quantitative measures of comparison between RG and PG at different coastal locations of India. The terms $N$, $a$, $b$, $d$, and $r$ are dimensionless, while the remaining terms have the units in cm.

<table>
<thead>
<tr>
<th>Location</th>
<th>$\bar{\text{RG}}$</th>
<th>$\bar{\text{PG}}$</th>
<th>$s_{\text{rg}}$</th>
<th>$s_{\text{pg}}$</th>
<th>$N$</th>
<th>$a$</th>
<th>$b$</th>
<th>MAE</th>
<th>RMSE</th>
<th>RMSE$_{a}$</th>
<th>RMSE$_{u}$</th>
<th>$d$</th>
<th>$r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Verem</td>
<td>0.00</td>
<td>0.00</td>
<td>48.72</td>
<td>48.53</td>
<td>72,788</td>
<td>-0.56</td>
<td>1.91</td>
<td>2.69</td>
<td>0.56</td>
<td>2.86</td>
<td>0.99</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>Tuticorin</td>
<td>0.00</td>
<td>0.00</td>
<td>20.92</td>
<td>20.58</td>
<td>38,082</td>
<td>-0.01</td>
<td>2.11</td>
<td>2.73</td>
<td>0.01</td>
<td>2.73</td>
<td>0.99</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>Mandapam</td>
<td>0.00</td>
<td>0.00</td>
<td>20.14</td>
<td>19.99</td>
<td>37,929</td>
<td>-0.01</td>
<td>1.11</td>
<td>1.46</td>
<td>0.01</td>
<td>1.47</td>
<td>0.99</td>
<td>0.99</td>
<td></td>
</tr>
</tbody>
</table>

![Scatter plots](image)

**Fig. 7** Scatter plots of sea-level measurements using RG versus PG along with linear fit shown as red line at (a) Verem, (b) Tuticorin, and (c) Mandapam. The percentage occurrence of the difference (PG–RG) along with respective RMSEs are marked with dashed lines at (d) Verem, (e) Tuticorin, and (f) Mandapam. $N$ is number of data points at respective station.
\[ H_n \cos(\sigma_n t - g_n), \]  

where \( H_n \) is an amplitude (cm), \( g_n \) is a phase lag (deg) on the equilibrium tide at Greenwich (local position in the present study), \( \sigma_n \) is an angular speed (degree per mean solar hour). Table 5 shows the main tidal constituents along with their description, time period (days), amplitudes (cm), and phase (deg) determined from the radar and pressure gauges during the study duration (see Fig. 8). The main diurnal and semi-diurnal tidal constituents are within ±2 mm in magnitude and within 1.5 deg in phase. However, the exception is the annual (Sa) and semi-annual (Ssa), for which the amplitudes (phases) differ by 10.7 (-3.2 deg) and 2.2 mm (11.8 deg), respectively. This could reflect, to some extent, the seasonal changes in the density of the water in the Mandovi estuary, from which measurements were collected, and could also be due to the limited data series of ~1 year duration.

Table 4  Statistical inferences from the difference between PG and RG measurements of sea level.

<table>
<thead>
<tr>
<th>Station</th>
<th>Verem</th>
<th>Tuticorin</th>
<th>Mandapam</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( d_0 )</td>
<td>( d_1 )</td>
<td>( d_0 )</td>
</tr>
<tr>
<td>Variance (cm²)</td>
<td>16.11</td>
<td>6.95</td>
<td>10.46</td>
</tr>
<tr>
<td>RMSE (cm)</td>
<td>4.02</td>
<td>2.69</td>
<td>3.24</td>
</tr>
</tbody>
</table>

\[ H_n \cos(\sigma_n t - g_n), \]  

Table 5  Major tidal constituents obtained from RG and PG deployed at Verem, Goa, during January 2009 to May 2010. For the details of harmonic tidal constituents, please refer to Pugh.  

<table>
<thead>
<tr>
<th>Tidal constituents</th>
<th>Time period (d)</th>
<th>Description of tidal constituents</th>
<th>Magnitude (cm)</th>
<th>Phase (deg)</th>
<th>Difference (mm)</th>
<th>Difference (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S_a )</td>
<td>365.2</td>
<td>Solar annual</td>
<td>6.65</td>
<td>7.72</td>
<td>-10.7</td>
<td>-3.2</td>
</tr>
<tr>
<td>( S_{sa} )</td>
<td>182.6</td>
<td>Solar semi-annual</td>
<td>3.71</td>
<td>3.49</td>
<td>2.2</td>
<td>11.8</td>
</tr>
<tr>
<td>( M_m )</td>
<td>27.55</td>
<td>Lunar monthly</td>
<td>2.06</td>
<td>1.68</td>
<td>3.8</td>
<td>1.4</td>
</tr>
<tr>
<td>( M_{mf} )</td>
<td>14.77</td>
<td>Variational fortnightly</td>
<td>1.33</td>
<td>1.15</td>
<td>1.8</td>
<td>6.7</td>
</tr>
<tr>
<td>( M_f )</td>
<td>13.66</td>
<td>Lunar fortnightly</td>
<td>1.27</td>
<td>1.31</td>
<td>-0.4</td>
<td>1.5</td>
</tr>
<tr>
<td>( Q_1 )</td>
<td>1.12</td>
<td>Larger elliptical lunar</td>
<td>3.02</td>
<td>2.98</td>
<td>0.4</td>
<td>-0.2</td>
</tr>
<tr>
<td>( O_{1} )</td>
<td>1.076</td>
<td>Principal lunar</td>
<td>14.82</td>
<td>14.75</td>
<td>0.7</td>
<td>0.0</td>
</tr>
<tr>
<td>( P_1 )</td>
<td>1.003</td>
<td>Principal solar</td>
<td>8.40</td>
<td>8.49</td>
<td>-0.9</td>
<td>0.3</td>
</tr>
<tr>
<td>( K_1 )</td>
<td>0.997</td>
<td>Luni-solar declinational diurnal</td>
<td>30.00</td>
<td>30.09</td>
<td>-0.9</td>
<td>-0.2</td>
</tr>
<tr>
<td>( J_{1} )</td>
<td>0.962</td>
<td>Elliptical lunar</td>
<td>1.71</td>
<td>1.71</td>
<td>0.0</td>
<td>0.7</td>
</tr>
<tr>
<td>( N_2 )</td>
<td>0.527</td>
<td>Larger elliptical lunar</td>
<td>12.14</td>
<td>12.20</td>
<td>-0.6</td>
<td>-0.4</td>
</tr>
<tr>
<td>( v_2 )</td>
<td>0.526</td>
<td>Larger evectional</td>
<td>2.41</td>
<td>2.34</td>
<td>0.6</td>
<td>-1.0</td>
</tr>
<tr>
<td>( M_2 )</td>
<td>0.518</td>
<td>Principal lunar</td>
<td>51.94</td>
<td>51.77</td>
<td>1.7</td>
<td>-0.3</td>
</tr>
<tr>
<td>( L_2 )</td>
<td>0.508</td>
<td>Smaller elliptical lunar</td>
<td>1.48</td>
<td>1.40</td>
<td>0.8</td>
<td>0.1</td>
</tr>
<tr>
<td>( S_2 )</td>
<td>0.5</td>
<td>Principal solar</td>
<td>18.37</td>
<td>18.22</td>
<td>1.4</td>
<td>-0.6</td>
</tr>
<tr>
<td>( K_2 )</td>
<td>0.499</td>
<td>Luni-solar declinational</td>
<td>4.74</td>
<td>4.74</td>
<td>0.0</td>
<td>-1.1</td>
</tr>
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Atmospheric pressure variations measured by the AWS at Dona Paula, Goa, are presented in Fig. 9(a). The atmospheric pressure anomaly shows annual cycle, where the atmospheric pressure is low (high) during June to July (January). The atmospheric pressure variations are within $\pm 10$ mb. The sea-level measurements obtained from the subsurface PG may lead to over- or underestimates, if atmospheric pressure corrections are not applied (inverse barometric effect $\sim -1$ cm/mbar). The sea level is first estimated from the PG without using measured atmospheric pressure, and instead, standard values such as $p_a = 1004.5$ mb, $\rho = 1.020$ g cm$^{-3}$, and $g = 980.665$ cm s$^{-2}$ were used [Eq. (1)]. Thus $d_0$ is the difference between the sea-level measurements obtained from PG and RG, where a constant value of barometric pressure is used in

\[ d_0 = \text{sea-level measurements from PG} - \text{sea-level measurements from RG}. \]

**Fig. 8** Major tidal constituents at Verem, Goa, obtained using RG and PG. (a) Amplitude and (b) phase.

Atmospheric pressure variations measured by the AWS at Dona Paula, Goa, are presented in Fig. 9(a). The atmospheric pressure anomaly shows annual cycle, where the atmospheric pressure is low (high) during June to July (January). The atmospheric pressure variations are within $\pm 10$ mb. The sea-level measurements obtained from the subsurface PG may lead to over- or underestimates, if atmospheric pressure corrections are not applied (inverse barometric effect $\sim -1$ cm/mbar). The sea level is first estimated from the PG without using measured atmospheric pressure, and instead, standard values such as $p_a = 1004.5$ mb, $\rho = 1.020$ g cm$^{-3}$, and $g = 980.665$ cm s$^{-2}$ were used [Eq. (1)]. Thus $d_0$ is the difference between the sea-level measurements obtained from PG and RG, where a constant value of barometric pressure is used in

\[ d_0 = \text{sea-level measurements from PG} - \text{sea-level measurements from RG}. \]

**Fig. 9** Time series of (a) atmospheric pressure (AP) anomaly (mb), (b) difference ($d_0$) between sea level estimated from pressure and radar gauge without measured atmospheric pressure correction, and (c) difference ($d_1$) between sea level estimated using PG and RG with measured atmospheric pressure correction.
estimating the sea level from PG [Fig. 9(b)]. This situation may arise when the sea-level measurements are made using pressure sensors at remote/offshore locations, where atmospheric pressure measurements are not available. With reference to Fig. 9(c), $d_1$ is the difference between the sea-level measurements obtained from PG and RG, wherein the measured barometric pressure is used in estimating the sea level from PG. The availability of atmospheric pressure data provides an excellent opportunity to estimate its effect on sea-level measurements obtained using PGs.

Table 4 presents the improvement in RMSEs at three study sites, when PG measurements are included with simultaneous barometric corrections. The difference ($d_0$) at Verem is shown in Fig. 9(b), with a variance of $\sim 16.1$ cm$^2$. The difference ($d_1$) between PG and RG with measured atmospheric pressure correction [Eq. (1)] is shown in Fig. 9(c). The variance in the difference reduces to $\sim 7.0$ cm$^2$. The RMSE for the difference with ($d_1$) and without ($d_0$) atmospheric pressure corrections is estimated to be 2.6 and 4.0 cm, respectively, as listed in Table 4. Similarly, the variation in $d_0$ at Tuticorin (Mandapam) is 10.46 (6.42) cm$^2$, which reduced to 7.48 (2.15) cm$^2$ for $d_1$.

5 Summary and Conclusions

The development of ICON consisting of sea-level gauges and AWS was initiated in the year 2005, immediately after the occurrence of December 2004 Sumatra tsunami, and the first real-/near-real-time reporting sea-level gauge based on pressure sensor was installed at Verem, Goa, in September 2005. However, presently all our sea-level stations use radar sensor, except at Verem, Goa, where both real-/near-real-time sea-level gauges based on radar and pressure sensors are in operation. This also meets the GLOSS recommendations to keep an overlapping period of at least 1 year to assess the reliability and accuracy of new equipment with enough data to make a comparison between the old and the new technology. In fact, the “perfect” sea-level gauge does not exist, and various technologies/options need to be evaluated for different applications. For example, PGs will be more suitable for deployment in offshore locations where height of the RG tower is a limitation and where there are jetties with high fishing activity.

This study describes a comparison of sea-level measurements from downward-looking aerial microwave radar and absolute subsurface PGs from Verem (Goa) and Tuticorin and Mandapam (Tamil Nadu), India. As recommended by Willmott, the comparisons of RG and PG are based on the difference measures and supported by graphical plots, RMSE, as well as systematic and unsystematic proportions or magnitudes. The results thus obtained suggest that both the systems function very well and produce similar tidal constituents. The sea-level measurements from subsurface PG with measured barometric pressure correction applied at Verem, Tuticorin, and Mandapam indicate an improvement in RMSE by 33%, 15%, and 42%, respectively, in the present study. However, during rainy season, the PG may underestimate the sea-level measurements due to water density variations resulting from fresh water influx from the river. For example, in a similar study at Verem from September 2007 to March 2009, Mehra et al. reported the variance of difference between the radar and absolute PG as 15.9 cm$^2$, which reduced to 5.7 and 4.0 cm$^2$, respectively, when atmospheric pressure alone and atmospheric pressure together with water density variations were introduced for obtaining sea level from an absolute PG. Also, Joseph et al. reported in a study at Marmugao Port, Goa, from June 1995 to July 1998 that the surface water density varied between 1.020 and 0.996 g cm$^{-3}$. During June to July 2008 at Verem sea-level gauge, which is located in the Mandovi estuary, the water density remained low ($\sim 1.000 \pm 0.005$ g cm$^{-3}$), and by September it increased to $\sim 1.020$ g cm$^{-3}$, remained at this level until May, and then sharply declined to $1.000 \pm 0.005$ g cm$^{-3}$ by June. The water density measurement site is $\sim 2.4$ km upstream from the PG location in the Mandovi estuary. The effective density used at Verem, Goa, is $1.020$ g cm$^{-3}$, $g = 980.665$ cm s$^{-2}$, and atmospheric pressure is obtained from AWS. However, the variations in the effective density $\sqrt{\rho} = (1.020 - 0.995) = 0.025$ g cm$^{-3}$ could lead to an underestimation of 2.45% in sea level by the PG. The long-term measurement of water density is practically difficult, but the importance of concurrent measurements of atmospheric pressure along with the PG measurements is duly emphasized in the present study.
It is worth mentioning that the sea-level station deployed for the present study measures the sea level in a completely different way than the traditional float or bubbler gauges. The ICON is developed with simple supporting structure to mount the sensors, powered by solar energy, and communicating data (using cellular modems) automatically to a base server located at CSIR-NIO, Goa. The system does not need expensive infrastructure, such as stilling-well, intake pipes, or cabins, normally seen in ports. However, these features could present some drawback, if the sites are exposed to harsh environment and lack security. With prior survey of the sites, the drawback of harsh environments and security aspects are minimized and we, therefore, have been able to operate the network of such stations (see http://inet.nio.org/) successfully since September 2005. The sea-level gauges at Verem and Kavaratti Island enabled real-time monitoring of the tsunami at Goa and Kavaratti Island due to the M_w 8.4 earthquake in Sumatra on September 12, 2007.31 In particular, sea-level gauges, surface meteorological instruments, and wave-rider buoys in the network enabled real-time monitoring of the response of west India coastal waters and Kavaratti lagoon to the November 2009 tropical cyclone Phyan.26 It is expected that relatively inexpensive and simple networks, similar to the one described in this paper, will be affordable to economically moderate institutions in their natural hazard mitigation efforts.

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References


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